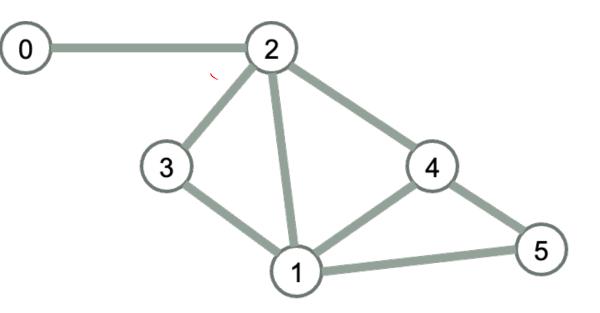
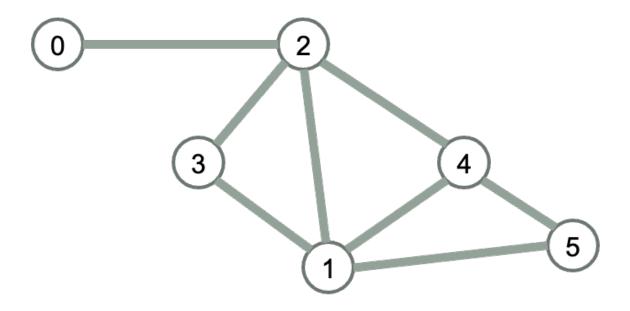
GRAPH SEARCH



Review: Adjacency list representation of graph

Vertex	adjList
0	
1	
2	
3	
4	
5	

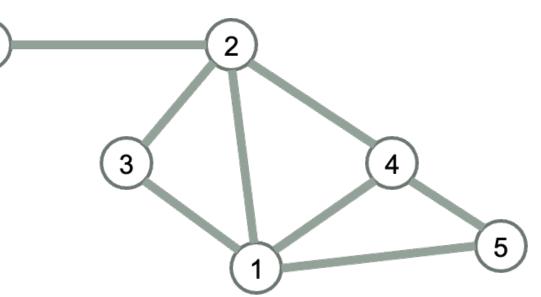


Which of these functions did you implement from last lecture's handout?

```
class graph{
public:
  graph(int n = 0) { // n is the number of vertices
      adjList = vector<list<int>>(n);
  }
  void addEdge(int from, int to);
```

```
A bool hasEdge(int i, int j) const;
```

B vector<bool> bfs(int source) const;



- bool isValidPath(const vector<int> & path) const; // returns true if the input path exists
- bool isReachable(int source, int dest) const; // returns true if a path exists from source to dest private:

0

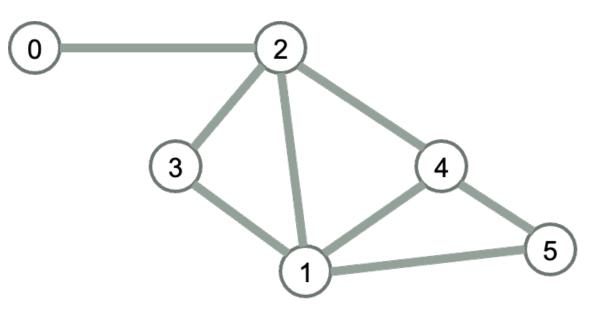
vector<list<int>> adjList;

E: All of them!

};

Link to hand out: <u>https://bit.ly/CS24F23GraphsHandout</u>

Breadth First Search: Sketch of Algorithm



- In general, a search algorithm would explore (or "visit") from a source vertex
 - all the vertices reachable,
 - never exploring out from the same vertex twice
- How does the BFS algorithm ensure this?

BFS Traverse: Time Complexity (express in terms of n, m)

Input: Graph G = (V, E), source vertex s, Let n = |V|, m = |E|

Start at source s;

Mark all the vertices as "not visited"

Mark s as visited

push s into a queue

while the queue is not empty:

- pop the vertex *u* from the front of the queue
 - for each of *u*'s neighbor (v)
 - If v has not yet been visited (v):
 - Mark v as visited
 - Push v in the queue
- How many times does the while loop run?
- How many times do we check if a vertex has been visited?

What is the time complexity of BFS? A. O(n)B. O(m)C. O(n + m)D. $O(n^2)$ E. None of the above

BFS Traverse: Time Complexity (express in terms of n, m)

- Input: Graph G = (V, E), source vertex s, Let n = |V|, m = |E|
- Start at source s;
- Mark all the vertices as "not visited"
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- push s into a queue
- while the queue is not empty:
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 - for each of *u*'s neighbor(v)
 - If v has not yet been visited (v):
 - Mark v as visited
 - Push v in the queue
- How many times does the while loop run?
- How many times do we check if a vertex has been visited?

BFS Traverse: Space Complexity (express in terms of n, m)

Input: Graph G = (V, E), source vertex s, Let n = |V|, m = |E|

Start at source s;

Mark all the vertices as "not visited"

Mark s as visited

push s into a queue

while the queue is not empty:

- pop the vertex *u* from the front of the queue
 - for each of *u*'s neighbor (v)
 - If v has not yet been visited (v):
 - Mark v as visited
 - Push v in the queue

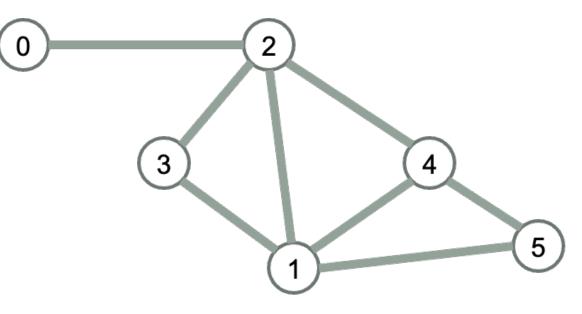
- Space complexity: Peak (additional) space usage expressed as big O

What is the space complexity of BFS? A. O(n)B. O(m)C. O(n + m)D. $O(n^2)$

E. None of the above

Application of BFS: shortest path

Vertex	dist	prev	adjList
0 (source)			2
1			2, 3, 4, 5
2			0, 1, 3, 4
3			1, 2
4			1, 2, 5
5			1, 4



Goal: Compute dist(v): fewest number of edges from the path from vertex **s** to **v**

BFS Shortest Path

Input: Graph G = (V, E), source vertex s, Let n = |V|, m = |E|

Start at source s;

Mark all the vertices as "not visited"

Mark s as visited

push s into a queue

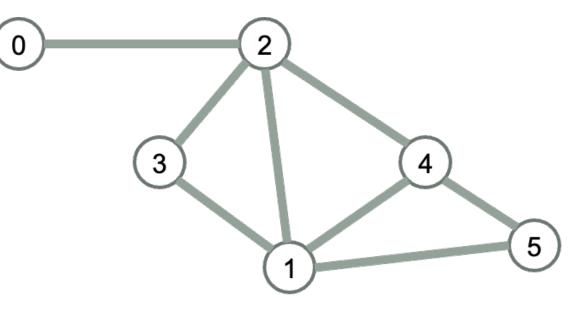
while the queue is not empty:

- pop the vertex *u* from the front of the queue
 - for each of *u*'s neighbor (v)
 - If v has not yet been visited (v):
 - Mark v as visited
 - Push v in the queue

- Modify BFS to compute the shortest path from source s to all other vertices

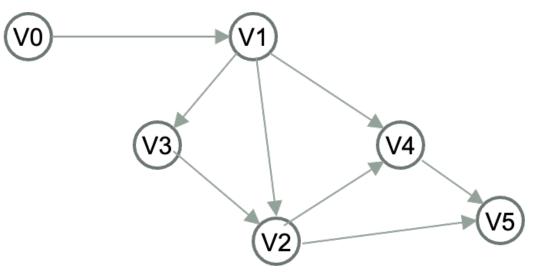
Depth First Search

Search as far down a single path as possible, backtrack as needed



Depth First Search

Search as far down a single path as possible, backtrack as needed



Assuming DFS chooses the lower number node to explore first, in what order does DFS visit the nodes in this graph? A. V0, V1, V2, V3, V4, V5 B. V0, V1, V3, V4, V2, V5 C. V0, V1, V3, V2, V4, V5 D. V0, V1, V2, V4, V5, V3

Work to complete your handout

class graph{

```
public:
```

```
graph(int n = 0) { // n is the number of vertices
  adjList = vector<list<int>>(n);
```

```
} void addEdge(int from, int to);
```

```
bool hasEdge(int i, int j) const;
```

```
vector<bool> bfs(int source) const;
```

bool isValidPath(const vector<int> & path) const; // returns true if the input path exists

bool isReachable(int source, int dest) const; // returns true if a path exists from source to dest

// (New!) Implement a variation of BFS to compute the shortest path from a source vertex to all vertices reachable from it

// (New!) Implement depth-first search

private:

```
vector<list<int>> adjList;
```

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