RUNNING TIME ANALYSIS OF BINARY SEARCH TREES

Problem Solving with Computers-II

include <iostream>
include <iostream>
iusing namespace std;
using namespace std;
int main(){
 cout<<"Hola Facebook\n";
 return 0;
}</pre>

What is the Big O of sumArray2

A. $O(N^2)$ B. O(N)

- C. O(N/2)
- D. O(log N)

E. None of the array

/* N is the length of the array*/
int sumArray2(int arr[], int N)

Running time of operations on sorted arrays: Discuss best case, worst case, average case

- Min :
- Max:
- Median:
- Successor:
- Predecessor:
- Search:
- Insert :
- Delete:

Binary Search Trees

- WHAT are the operations supported?
- HOW do we implement them?
- WHAT are the (worst case) running times of each operation?

Visualize BST operations: <u>https://visualgo.net/bn/bst</u>

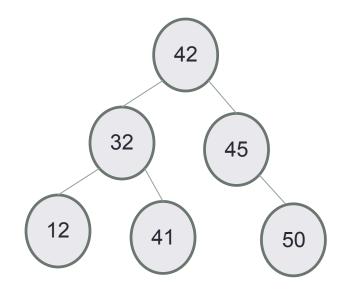
Height of the tree



Many different BSTs are possible for the same set of keys Examples for keys: 12, 32, 41, 42, 45

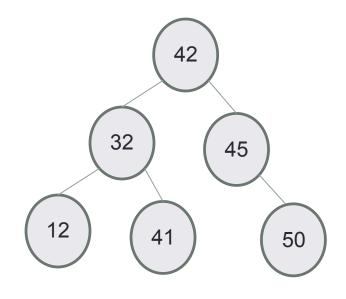
- Path a sequence of nodes and edges connecting a node with a descendant.
- A path starts from a node and ends at another node or a leaf
- Height of node The height of a node is the number of edges on the longest downward path between that node and a leaf.

Worst case Big-O of search



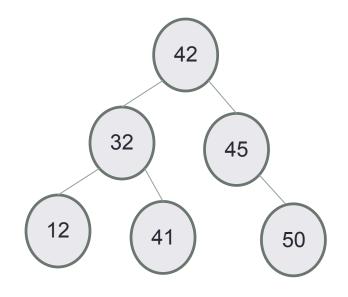
- Given a BST of height H and N nodes, what is the worst case complexity of searching for a key?
 A. O(1)
 B. O(log N)
 C. O(H)
- D. O(log H)

Worst case Big-O of insert



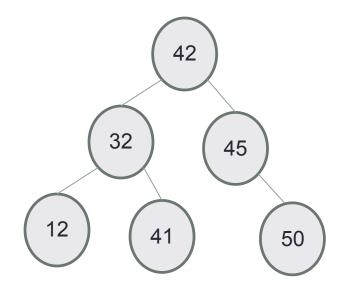
- Given a BST of height H and N nodes, what is the worst case complexity of inserting a key?
- A. O(1)
- B. O(log N)
- C. O(H)
- D. O(log H)

Worst case Big-O of min/max



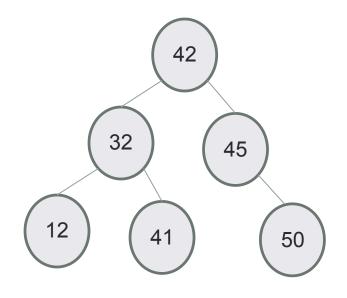
- Given a BST of height H and N nodes, what is the worst case complexity of finding the minimum or maximum key?
- A. O(1)
- B. O(log N)
- C. O(H)
- D. O(log H)

Worst case Big-O of predecessor/successor



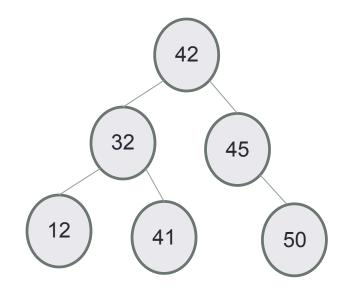
- Given a BST of height H and N nodes, what is the worst case complexity of finding the minimum or maximum key?
- A. O(1)
- B. O(log N)
- C. O(H)
- D. O(log H)

Worst case Big-O of delete



- Given a BST of height H and N nodes, what is the worst case complexity of deleting the key (assume no duplicates)?
- A. O(1)
- B. O(log N)
- C. O(H)
- D. O(log H)

Big O of traversals

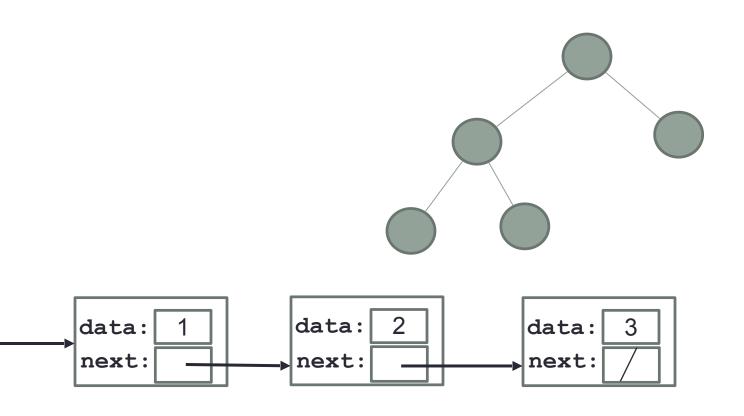


In Order: Pre Order: Post Order:

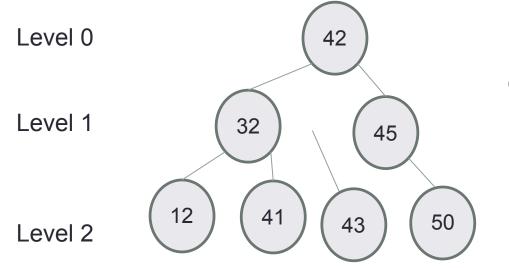
Worst case analysis

Are binary search trees *really* faster than linked lists for finding elements?

- A. Yes
- B. No

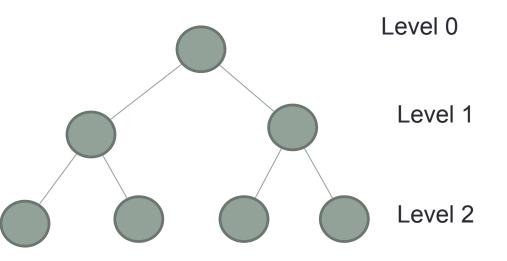


Completely filled binary tree



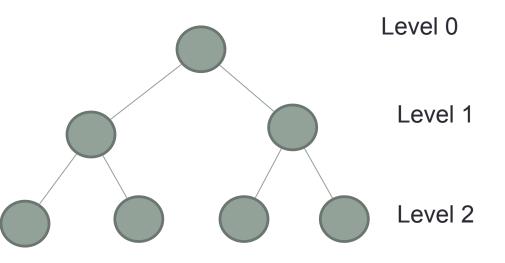
Nodes at each level have exactly two children, except the nodes at the last level

Relating H (height) and N (#nodes) find is O(H), we want to find a f(N) = H



How many nodes are on level L in a completely filled binary search tree? A.2 B.L C.2*L D.2^L

Relating H (height) and N (#nodes) find is O(H), we want to find a f(N) = H



Finally, what is the height (exactly) of the tree in terms of N?

Balanced trees

- Balanced trees by definition have a height of O(log N)
- A completely filled tree is one example of a balanced tree
- Other Balanced BSTs include AVL trees, red black trees and so on
- Visualize operations on an AVL tree: <u>https://visualgo.net/bn/bst</u>

Summary of operations

Operation	Sorted Array	Binary Search Tree	Linked List
Min			
Max			
Median			
Successor			
Predecessor			
Search			
Insert			
Delete			

CHANGING GEARS: C++STL

- The C++ Standard Template Library is a very handy set of three built-in components:
 - Containers: Data structures
 - Iterators: Standard way to search containers
 - Algorithms: These are what we ultimately use to solve problems

C++ STL container classes

array vector forward list list stack queue priority queue set multiset (non unique keys) deque unordered set map unordered map multimap bitset