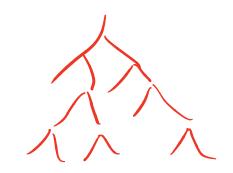
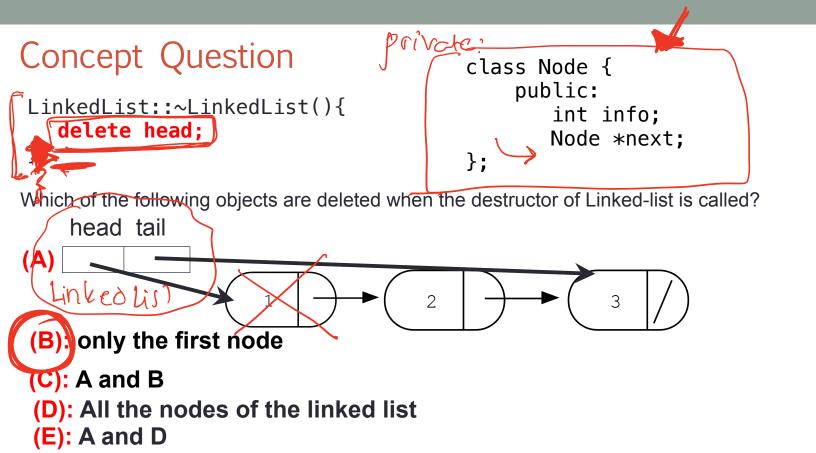
BINARY SEARCH TREES



Problem Solving with Computers-II



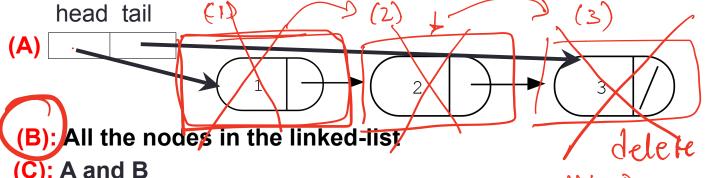


Concept question

_inkedList::~LinkedList(){ delete head;

The last call Node::~Node(){ delete next; delete 0;

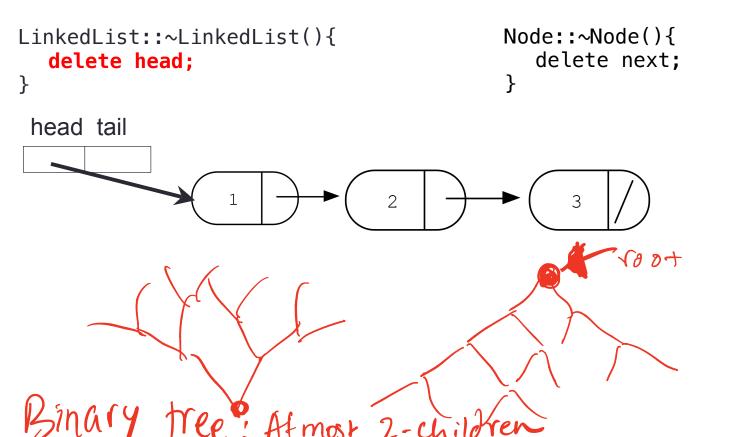
Which of the following objects are deleted when the destructor of Linked-list is called?

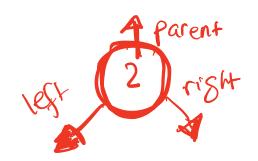


(C): A and B

(D): Program crashes with a segmentation fault

(E): None of the above





Class Node &

public:
int data;

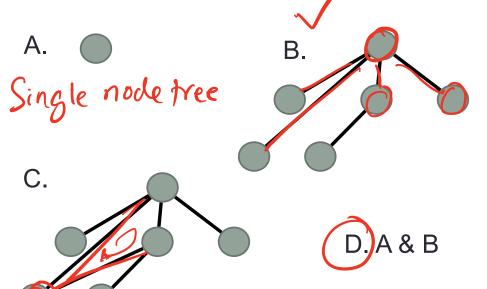
Node * Parent;

Node * left;

Node * right;

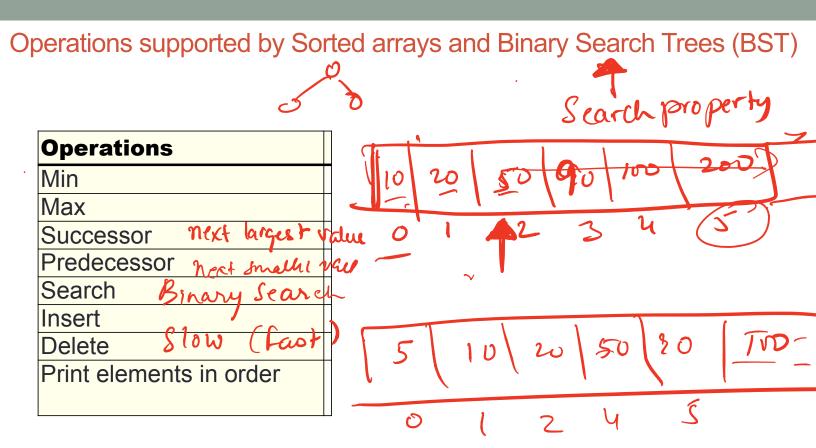
Which of the following is/are, a tree?

root = 0 empty tree

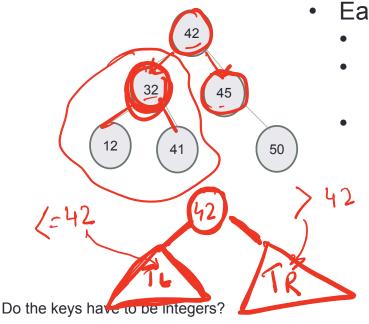


E. All of A-C

Binary Search Trees (Variant) + Red-Blacks What are the operations supported? insert, delete, search, nue Vanilla! What are the running times of these operations? Build intuition - Complexity How do you implement the BST i.e. operations supported by it?



Binary Search Tree – What is it?

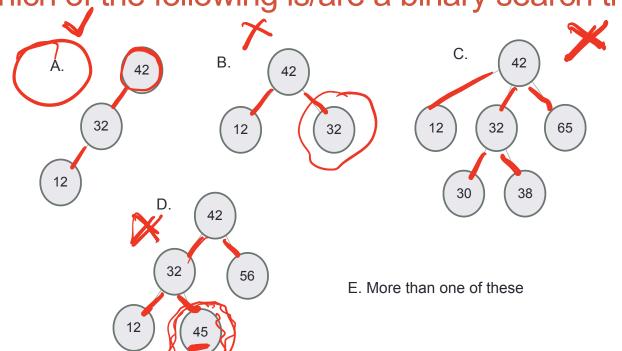


- Each node:
 - stores a key (k)
 - has a pointer to left child, right child and parent (optional)
 - Satisfies the Search Tree Property

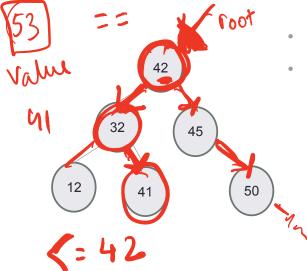
For any node, Keys in node's left subtree <= Node's key Node's key < Keys in node's right subtree

(355)

Which of the following is/are a binary search tree?



BSTs allow efficient search!



- Start at the root;
- Trace down a path by comparing **k** with the key of the current node x:
 - If the keys are equal: we have found the key
 - If $\mathbf{k} < \text{key}[\mathbf{x}]$ search in the left subtree of \mathbf{x}
 - If k > key[x] search in the right subtree of x

A node in a BST

```
class BSTNode {
public:
                               initializer list
  BSTNode* left;
  BSTNode* right;
  BSTNode* parent;
  int const data;
  BSTNode (const int & d) : data(d) {
    left = right = parent = 0;
```

Define the BST ADT Abstract Data Type

Operations	
Search	42
Insert	
Min	
Max	$\begin{pmatrix} 32 \end{pmatrix} \begin{pmatrix} 45 \end{pmatrix}$
Successor	
Predecessor	
Delete	$\begin{pmatrix} 12 \end{pmatrix} \begin{pmatrix} 41 \end{pmatrix} \begin{pmatrix} 50 \end{pmatrix}$
Print elements in order	

Traversing down the tree

Suppose n is a pointer to the root. What is the output of the following code:

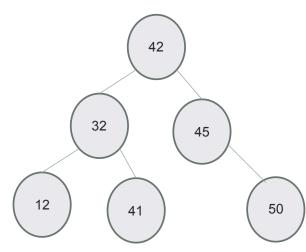
```
n = n - > left;
n = n->right;
cout<<n->data<<endl;
 A. 42
```

B. 32

C. 12

D. 41

E. Segfault

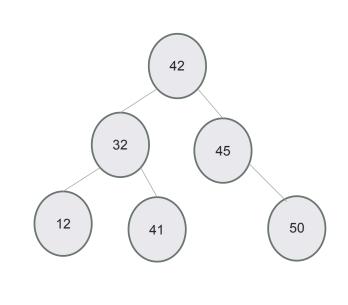


Traversing up the tree

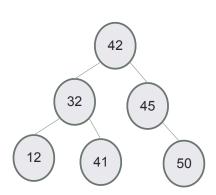
E. Segfault

- Suppose n is a pointer to the node with value 50.
- What is the output of the following code:

```
n = n-parent;
  = n->parent;
n = n - > left;
cout<<n->data<<endl;
A. 42
 B. 32
 C. 12
 D. 45
```



Insert

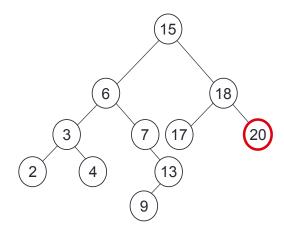


- Insert 40
- Search for the key
- Insert at the spot you expected to find it

Max

Goal: find the maximum key value in a BST Following right child pointers from the root, until a leaf node is encountered. The least node has the max value

Alg: int BST::max()



Maximum = 20

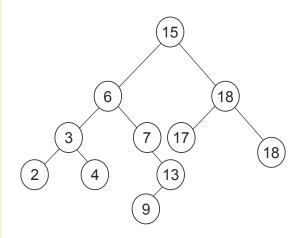
Min

Goal: find the minimum key value in a BST Start at the root.

Follow _____ child pointers from the root, until a leaf node is encountered

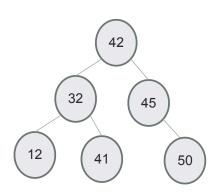
Leaf node has the min key value

Alg: int BST::min()



Min = ?

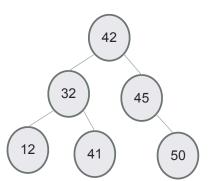
In order traversal: print elements in sorted order



Algorithm Inorder(tree)

- 1. Traverse the left subtree, i.e., call Inorder(left-subtree)
- 2. Visit the root.
- 3. Traverse the right subtree, i.e., call Inorder(right-subtree)

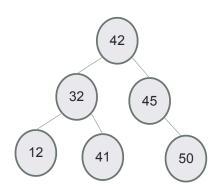
Pre-order traversal: nice way to linearize your tree!



Algorithm Preorder(tree)

- 1. Visit the root.
- 2. Traverse the left subtree, i.e., call Preorder(left-subtree)
- 3. Traverse the right subtree, i.e., call Preorder(right-subtree)

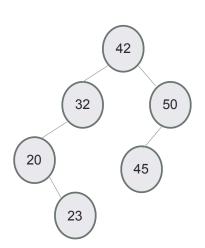
Post-order traversal: use in recursive destructors!



Algorithm Postorder(tree)

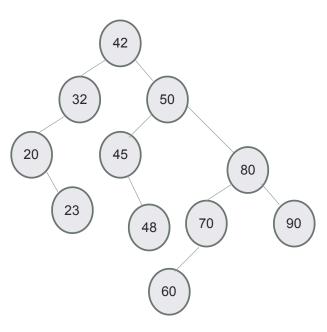
- 1. Traverse the left subtree, i.e., call Postorder(left-subtree)
- 2. Traverse the right subtree, i.e., call Postorder(right-subtree)
- 3. Visit the root.

Predecessor: Next smallest element



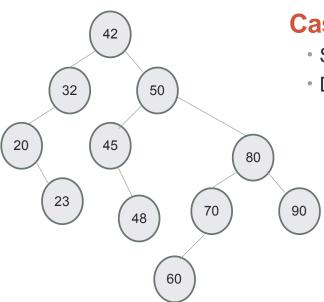
- What is the predecessor of 32?
- What is the predecessor of 45?

Successor: Next largest element



- What is the successor of 45?
- What is the successor of 50?
- What is the successor of 60?

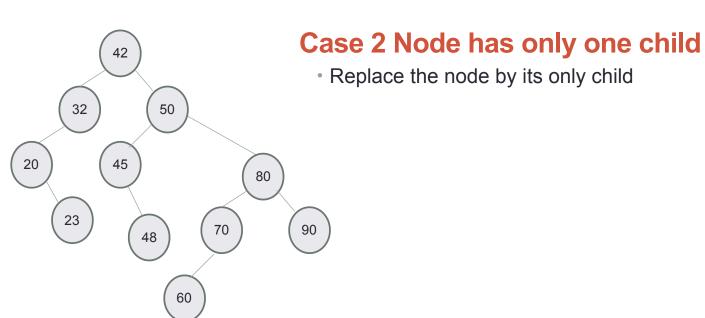
Delete: Case 1



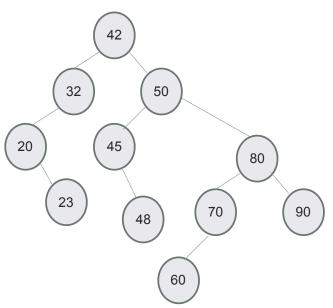
Case 1: Node is a leaf node

- Set parent's (left/right) child pointer to null
- Delete the node

Delete: Case 2



Delete: Case 3



Case 3 Node has two children

 Can we still replace the node by one of its children? Why or Why not?

Binary Search

- Binary search. Given value and sorted array a[], find index i such that a[i] = value, or report that no such index exists.
- Invariant. Algorithm maintains a [lo] ≤ value ≤ a [hi].
- Ex. Binary search for 33.

