

STACK AND QUEUE

Problem Solving with Computers-II

C++

```
#include <iostream>
using namespace std;

int main(){
    cout<<"Hola Facebook!";
    return 0;
}
```

C++STL

- The C++ Standard Template Library is a very handy set of three built-in components:
 - Containers: Data structures
 - Iterators: Standard way to search containers
 - Algorithms: These are what we ultimately use to solve problems

C++ STL container classes

```
array  
vector  
forward_list  
list  
set  
stack  
queue  
priority_queue  
multiset (non unique keys)  
deque  
unordered_set  
map  
unordered_map  
multimap  
bitset
```

Stacks – container class available in the C++ STL

- Container class that uses the Last In First Out (LIFO) principle
- Methods
 - i. `push()`
 - ii. `pop()`
 - iii. `top()`
 - iv. `empty()`

Lab05: Evaluate a fully parenthesized infix expression

$(4 * ((5 + 3.2) / 1.5))$ // okay

$(4 * ((5 + 3.2) / 1.5)$ // unbalanced parens - missing last ')'

$(4 * (5 + 3.2) / 1.5))$ // unbalanced parens - missing one '('

$4 * ((5 + 3.2) / 1.5)$ // not fully-parenthesized at '*' operation

$(4 * (5 + 3.2) / 1.5)$ // not fully-parenthesized at '/' operation

Checking if the parenthesis are balanced

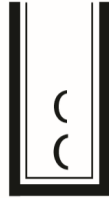
Initial
empty
stack



Read
and push
first (



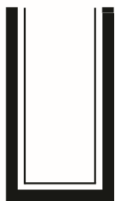
Read
and push
second (



$((2 * 2) + (8 + 4))$

Checking if the parenthesis are balanced

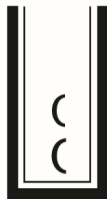
Initial
empty
stack



Read
and push
first (



Read
and push
second (



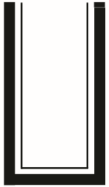
$((2 * 2) + (8 + 4))$

What should **be the next step after the first right parenthesis is encountered?**

- A. Push the right parenthesis onto the stack
- B. If the stack is not empty pop the next item on the top of the stack
- C. Ignore the right parenthesis and continue checking the next character
- D. None of the above

$$((2 * 2) + (8 + 4))$$

Initial
empty
stack



Read
and push
first (



Read
and push
second (



Read first
) and pop
matching (



Read
and push
third (



Read
second)
and pop
matching (



Read third
) and pop
the last (



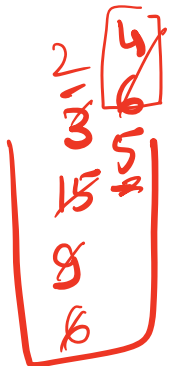
Evaluating a fully parenthesized infix expression

evaluate

$$(((6) + 9) / 3) * (6 - 4)$$

0 1 2 3 4 5 6

↑ ↑ ↑ ↑ ↑ ↑



nums

Stack<int> num



operations

Stack<char> op

10

- A. One stack
- B. Two stacks
- C. Three or more

Evaluating a fully parenthesized infix expression

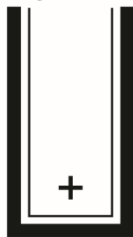
Characters read so far (shaded):

$((6 + 9) / 3) * (6 - 4)$

Numbers



Operations

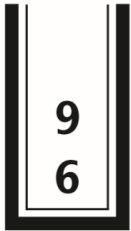


Evaluating a fully parenthesized infix expression

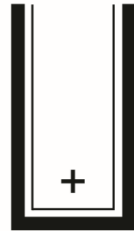
Characters read so far (shaded):

`(((6 + 9) / 3) * (6 - 4))`

Numbers



Operations



→
6 + 9 is 15

Numbers



Operations



Before computing 6 + 9

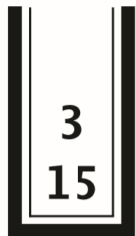
After computing 6 + 9

Evaluating a fully parenthesized infix expression

Characters read so far (shaded):

`(((6 + 9) / 3) * (6 - 4))`

Numbers



Before computing $15/3$

Operations



$15 / 3$ is 5

Numbers



After computing $15/3$

Operations



Notations for evaluating expression

- **Infix** number operator number
- (Polish) Prefix operators precede the operands
- (Reverse Polish) Postfix operators come after the operands

$$7 + 5$$

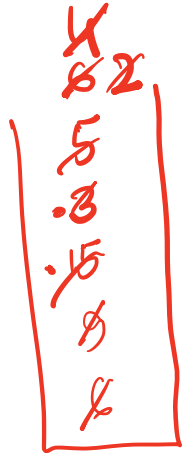
$$+ 7 5$$

$$7 5 +$$

$$7 5 +$$

Evaluating post fix expressions using a single stack

Postfix: $6, 9, +, 3, /, 6, 4, -, *$



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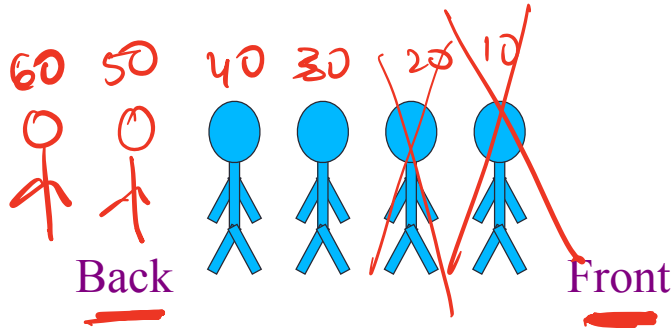
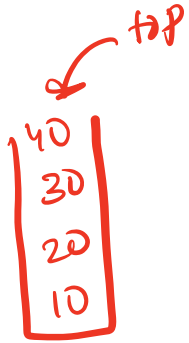
15 / 3
a b

Infix: $((6 + 9) / 3) * (6 - 4)$

Stack <int> num

Queue Operations

- A queue is like a queue of people waiting to be serviced
- The queue has a **front** and a **back**.



STL
queue<int>q;

q.push(50)
q.push(60)

q.back()

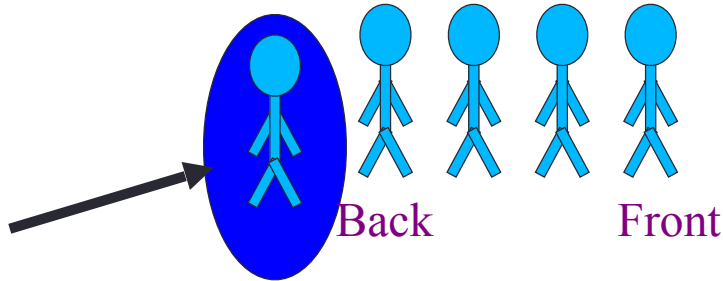
q.front()

q.pop()

// deleting the
front element
q.empty()

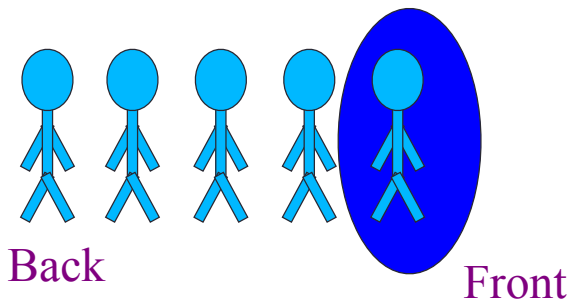
Queue Operations

- New people must enter the queue at the back. The C++ queue class calls this a **push**, although it is usually called an **enqueue** operation.



Queue Operations

- When an item is taken from the queue, it always comes from the front. The C++ queue calls this a **pop**, although it is usually called a **dequeue** operation.

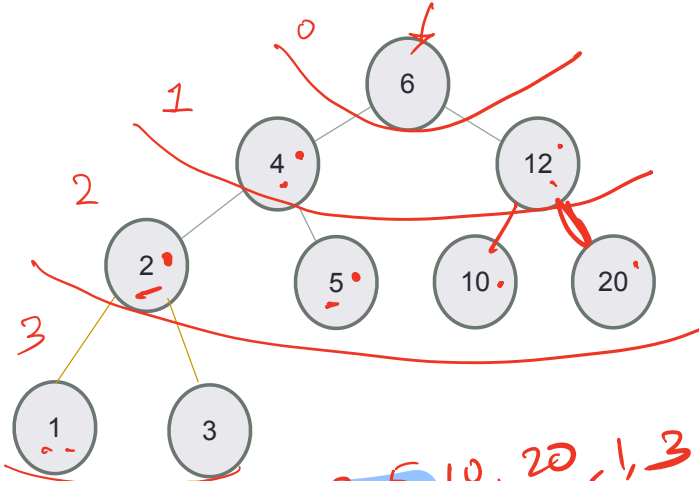


Queue Class

- The C++ standard template library has a queue template class.
- The template parameter is the type of the items that can be put in the queue.

```
template <class Item>  
class queue<Item>  
{  
public:  
    queue( );  
    void push(const Item& entry);  
    void pop( );  
    bool empty( ) const;  
    Item front( ) const;  
    ...
```

Breadth first traversal



Algo BFS.

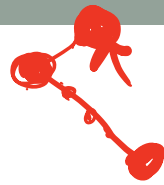
- Take an empty Queue.
- Start from the root, insert the root into the Queue.
- Now while Queue is not empty,
 - Extract the node from the Queue and insert all its children into the Queue. (if they exist)
 - Print the extracted node.

6, 4, 12, 2, 5, 10, 20, 1, 3
 6, 4, 12, 2, 5, 10, 20, 1, 3

~~3, 2, 20, 10, 5, 12, 4, 6~~ front

Summary of operations

$n \leftarrow$ no. of keys



Operation	Sorted Array	Binary Search Tree		Linked List		Stack	Queue
	worst case	regular	balanced (self sorted)	sorted	unsorted		
Min	$O(1)$	$O(n)$	$O(\log n)$			X	X
Max	$O(1)$	$O(n)$	$O(\log n)$			X	X
Median	$O(1)$	$O(n)$	$O(n)$			X	X
Successor	$O(1)$	$O(n)$	$O(\log n)$			X	X
Predecessor	$O(1)$	$O(n)$	$O(\log n)$			X	X
Search	$O(\log n)$	$O(n)$	$O(\log n)$			X	X
Insert	$O(n)$	$O(n)$	$O(\log n)$			$O(1)$	$O(1)$
Delete	$O(n)$	$O(n)$	$O(\log n)$			$O(1)$	$O(1)$

